

# Course Guide: MATHEMATICS



CHEMISTRY DEGREE COMPLUTENSE UNIVERSITY OF MADRID ACADEMIC YEAR 2019-2020

# **Mathematics**



# **I.- IDENTIFICATION**

COURSE NAME: CHARACTER: SUBJECT: MODULUS: DEGREE: SEMESTER/TERM TAUGHT: DEPARTAMENT: Mathematics Mandatory Mathematics Basic Bachelor in Chemistry First term (first year) Department of Applied Mathematics and Mathematical Analysis

## **LECTURER:**

Grupo D					
Theory Seminar Tutorial	Lecturer: Department: Office: e-mail:	ROSA PARDO Applied Mathematics and Mathematical Analysis QB-648 <u>rpardo@ucm.es</u>			

# **II.- OBJECTIVES**

## **GENERAL OBJECTIVES**

This subject is the first contact of the student at the university with the language of science, Mathematics. Therefore, the main target is to train the student to atain the essential skills for using and understanding this language, while achieving fundamental knowledge on differential and integral calculus, as well as the control of its main techniques.

## SPECIFIC OBJECTIVES

- Knowledge and control of the technique of derivation and integration of functions of one and several variables.
- Knowledge of the approximation of functions by means of series of powers.
- Solutions of differential equations.

# **III.- MODULE PREREQUISITES AND RECOMMENDATIONS**

# PREVIOUS KNOWLEDGE:



The knowledge described in the official programs of the subjects of Mathematics in the pre-university academic courses for a science student. In particular, it is recommended to know the derivation, integration, and graphical representation of functions of a real variable.

#### **RECOMMENDATIONS:**

In case the student do not possess the required prerequisites, it is strongly recommended to acquire them before starting this lecture.

## **IV.- CONTENTS**

## **BRIEF DESCRIPTION:**

Functions of one and several variables. Derivation, integration, and graphical representation. Power series. Convergence criteria. Taylor, Series expansion. Differential equations.

## **SYLLABUS:**

#### 1. Differential Calculus

- Differentiation rules. Derivative of inverse functions. Chain rule. Implicit differentiation.
- Tangent lines. Classification of critical points.
- Graphical representation of functions of one variable.
- Level curves. Graphical representation of functions of two variables.
- Partial derivatives. Gradient vector and tangent plane. The Hessian matrix; classification of critical points. Constrained maximum and minimum; Lagrange multipliers.

- Exact differential. Finding *a* potential function of a conservative vector field.

#### 2. Integral Calculus

- Primitive of a function. Integration by parts, changes of variable, rational functions.

- Fundamental theorem of calculus.
- Multiple integrals. Fubini's theorem. Change of Variable, the Jacobian matrix. Polar coordinates.
- Applications of the integral.

#### 3. Power Series

- Convergence criteria.
- Expansion of a function in power series. Radius of convergence



## 4. Differential equations

- Elementary methods of resolution. Separation of variables, exact equations, integrating factor, linear equations.
- Second order linear equations. Undetermined coefficients and power series solutions.

# **V.- COMPETENCES**

## **GENERAL:**

- **CG6:** To analyse and solve qualitative and quantitative problems..
- CG7: To recognise, analyse new problems developping strategies for their resolution.

#### **SPECIFIC:**

0	CE26-M1:	To use the language of mathematics.
0	CE26-M2:	To derive functions of one and several variables.
0	CE26-M3:	To represent functions of one and several variables graphically.
0	CE26-M4:	To integrate functions of one and several variables.
0	CE26-M5:	To expand functions power series.
0	CE27-M1:	To solve differential equations.

## **GENERIC:**

0	СТ2:	To work in team.
0	СТ3:	To show criticism (including self-criticism) towards any kind of
		reasoning.
0	<b>CT4:</b>	To be able to adapt to new situations.

# **VI.- LEARNING OUTCOMES**

Having passed the course, students should be able to:

- Precisely handle the mathematical language (symbols, formulas, equations, ...).
- Calculate the derivatives of functions of one and several variables.
- Classify the critical points of one and two variable functions.
- Calculate the maximum and minimum of a function of one and several variables.
- Graphically represent functions of one and two variables.
- Know the concept of integral and its relationship with the concepts of area and volume.
- $\circ\,$  Use correctly the properties of the integral and the fundamental theorems of the calculation.
- Use the most usual integration methods in the calculation of primitives of functions of one and several variables.



- Handle the most common criteria of convergence of numerical series.
- Calculate the Taylor developments of a function.
- Calculate the radius of convergence of a series of powers.
- Manage the methods of solving ordinary differential equations of the most common first order.
- Apply the technique of indeterminate coefficients for the resolution of linear secondorder equations with constant coefficients.
- Obtain solutions in the form of power series for linear differential equations.

# **VII. – WORKING HOURS, DISTRIBUTED BY ACTIVITY**

The subject of Mathematics is a subject of the Basic Module of the Degree in Chemistry, with an allocation of 9 credits that are taught throughout the first term. The dedication of the student to this subject will be, according to ECTS criteria, 225 hours a year, distributed as follows:

Actividad	Attendence (hours)	Self study (hours)	Credits	
Lectures	49	91	5,6	
Seminars	18	22	1,6	
Tutorials	3	4	0,3	
Preparation of exams	6	32	1,5	
Total	76	149	9	

# **VIII.- METHODOLOGY**

At the start of the course, during the first (**face to face**) class, the student will be informed by the Lecturer the content of this course.

Exercises will be published on the virtual campus in order to encourage the students to try to solve them individually.

The so called seminars and tutorials are face to face lectures, dedicated to the resolution of the exercises.

# **IX.- BIBLIOGRAPHY**

## **BASIC:**

• RODRÍGUEZ SALAZAR, S.: "Matemáticas para estudiantes de Químicas", Síntesis, 2007.

# **Course Guide:**



- FERREIRA, R. y RODRIGUEZ SALAZAR, S.: "Ecuaciones diferenciales y cálculo vectorial", Garceta, 2013
- STEINER, ERICH: "The Chemistry Maths Book", Oxford University Press, 2008.
- SALAS-HILLE: "Calculus : one and several variables", John Wiley, 2006.
- ZILL, D. G.: "A FIRST COURSE IN DIFFERENTIAL EQUATIONS with Modeling Applications", Grupo editorial Iberoamericana, 1994.

## **COMPLEMENTARY:**

- BOYCE, W.; Di PRYMA, R. C.: "Elementary Differential Equations and Boundary Value Problems", John Wiley & Sons, 2.017.
- LÓPEZ-GÓMEZ, J.: "*Ecuaciones diferenciales y variable compleja: problemas y ejercicios resueltos*", Prentice Hall, Madrid, 2002.

# X.- ASSESSMENT PROCEDURE

20% of the mark will come from a short exam during the course and 80% from a 3 hour end of semester exam.

**EXAMS:** 

100%

100%

- A 1 hour exam will be hold during the course (20% of the final score).
- The **final exam** will last 3 hours and will contribute 80% to the final score

The evaluation concerns subjects CG6, CG7, CE26, CE27, CT2, CT3 y CT4.

## **RESIT EXAMINATION IN JULY:**

- If a student fails the exams, the student has to attend a resit exam, which will last for three hours, concerning all the subjects of the course and will take place in July. This exam corresponds to 100% of the final mark.

The students will be informed about the results of the 1 hour exam in due time which would allow the students to prepare this exam and also to organise his other studies accordingly. In any case, the students will be informed about their qualification in a period which should not exceed 20 days after the exam.



# **ACTIVITIES SCHEDULE**

UNITS	ACTIVITY	HOURS	GROUPS	START	END	
1. Differencial Calculus	Lectures	11	1	1st Week	3rd Week	
1. Differencial Calculus	Exercises	4	1	Ist week	SIU WEEK	
2 Integral Calculus	Lectures	14	1	4th Week	7th Week	
2. Integral Calculus	Exercises	6	1	4ui week	/III WEEK	
3. Power series	Lectures	7	1	8th Week	9th Week	
5. Power series	Exercises	3	1	our week	9th week	
4 Differencial Equations	Lectures	17	1	10th Week	144 Weels	
4. Differencial Equations	Exercises	8	1	Toth week	14th Week	
	Written Exams	6		Determined by the «Faculty (School)»		

\* The supervised tutorials/activities are subject to possible modification depending on the complete organisation of the course



# **SUMMARY OF THE ACTIVITIES**

Lecture activities	Associated Competences	Lecturer Activity	Student Activity	Assessment procedure	Р	NP	Total	С	
Face to face classes for theory	CG6, CG7	Outlining the subjects of the lectures	Listing, understanding, planning questions. Note taking, for clarifying doubts.	Short and long exams.	49			80%	
Face to face classes for exercises	CE26, CE27 CT2, CT3, CT4	Apply the theory learned to the resolutions of exercises.	Presenting solution to exercises. Planning of questions. Presentations on the blackboard.	Short and long exams.	18			- + 20%	
Tutorials	CG6, CG7 CE26, CE27 CT2, CT3, CT4	Help the student to organise his studies.	Consulting the lecturer about the difficulties the student may encounter, both conceptual and methodological, when studying the subject.	Mandatory attendance on assigned days.	3	149			
Exams	012, 013, 014	Proposal, surveillance and correction of the exam. Assessment of the student.	Preparation and accomplishment.	Short and long exams.	6				
P : In class; NP: Self studies; C: evaluation									